

Capture Zone Analysis



<http://www.spokaneriverrescue.com/images/rescue-helo061.JPG>

Capture Zone Analysis Confined Aquifer

The equation to describe the edge of the capture zone for a confined aquifer when steady-state conditions have been reached is (Todd 1980; Grubb 1993):

$$x = \frac{-y}{\tan(2\pi Kbiy/Q)} \quad (10.16)$$

where

x and y are directions defined on Figure 10.32

Q is the pumping rate (L^3/T ; ft^3/day or m^3/day)

K is the hydraulic conductivity (L/T ; ft/day or m/day)

b is the initial saturated thickness of the aquifer (L ; ft or m)

i is the hydraulic gradient of the flow field in the absence of the pumping well (dimensionless)

$\tan(y)$ is in radians

Capture Zone Analysis Confined Aquifer

$$x_0 = -Q/(2\pi Kbi) \quad (10.17)$$

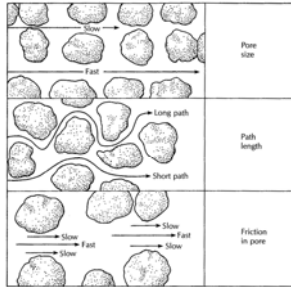
where x_0 is the distance from the pumping well to the down-gradient edge of the capture zone (L ; ft or m).

2. The maximum width of the capture zone as x approaches infinity is given by

$$y_{max} = \pm Q/(2Kbi) \quad (10.18)$$

where y_{max} is the half-width of the capture zone as x approaches infinity.

Longitudinal Dispersion



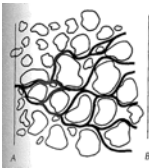
▲ FIGURE 10.8
Factors causing pore-scale longitudinal dispersion.

Lateral Dispersion

Lateral dispersion is caused by the fact that, as a fluid containing a contaminant flows through a porous medium, the flow paths can split and branch out to the side. This will occur even in the laminar flow conditions that are prevalent in ground-water flow (Figure 10.9).

The mechanical dispersion due to the preceding factors is equal to the product of the average linear velocity and a factor called the dynamic dispersivity (a_L).

$$\text{Mechanical dispersion} = a_L v_x \quad (10.5)$$



◀ FIGURE 10.9
Flow paths in a porous medium that cause lateral hydrodynamic dispersion.

Hydrodynamic Dispersion

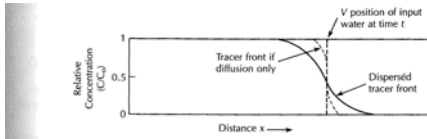
The processes of molecular diffusion and mechanical dispersivity cannot be separated in flowing ground water. Instead, a factor termed the coefficient of hydrodynamic dispersion, D_L , is introduced. It takes into account both the mechanical mixing and diffusion. For one-dimensional flow it is represented by the following equation:

$$D_L = a_L v_x + D^* \quad (10.6)$$

where

- D_L = the longitudinal coefficient of hydrodynamic dispersion
- a_L = the dynamic dispersivity
- v_x = the average linear ground-water velocity
- D^* = the effective molecular diffusion coefficient

Diffusion/Dispersion and Breakthrough of a solute



▲ FIGURE 10.10 Influence of dispersion and diffusion on "breakthrough" of a solute.

Advection and Dispersion

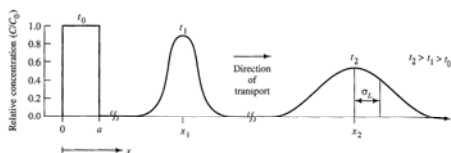
The one-dimensional equation for hydrodynamic dispersion (Beruch & Street 1967; Hoopes & Harleman 1967) is given by

$$D_L \frac{\partial^2 C}{\partial x^2} - v_x \frac{\partial C}{\partial x} = \frac{\partial C}{\partial t} \quad (10.7)$$

where

- D_L is the coefficient of longitudinal hydrodynamic dispersion
- C is the solute concentration
- v_x is the average ground-water velocity in the x -direction
- t is the time since start of solute invasion

Advection and Dispersion



▲ FIGURE 10.11 Transport and spreading of a solute slug with time due to advection and dispersion. A slug of solute was injected at $x = 0 + a$ at time t_0 with a resulting concentration of C_0 . The ground-water flow is to the right. Source: C. W. Fetter, *Contaminant Hydrogeology*. Upper Saddle River NJ: Prentice Hall, 1999.

Advection and Dispersion

The concentration, C , at some distance, L , from a constant source of contamination at concentration, C_0 , at time, t , is given by the following expression (Ogata 1970), where erfc is the complementary error function:

$$C = \frac{C_0}{2} \left[\text{erfc} \left(\frac{L - v_x t}{2\sqrt{D_L t}} \right) + \exp \left(\frac{v_x L}{D_L} \right) \text{erfc} \left(\frac{L + v_x t}{2\sqrt{D_L t}} \right) \right] \quad (10.8)$$

where

C is the solute concentration (M/L^3 , mg/L)

C_0 is the initial solute concentration (M/L^3 , mg/L)

L is the flow path length (L ; ft or m)

v_x is the average linear ground-water velocity (L/T ; ft/day or m/day)

t is the time since release of the solute (T ; day)

D_L is the longitudinal dispersion coefficient (L^2/T ; ft²/s or m²/s)

Advection and Dispersion

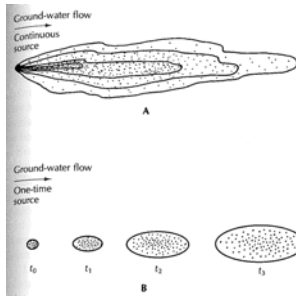


FIGURE 10.12
A. The development of a contamination plume from a continuous point source. B. The travel of a contaminant slug from a one-time point source. Density of dots indicates solute concentration.

Length Dependence of Dispersion

apparent longitudinal dynamic dispersivity and flow length, and found that the following equation best describes the relationship.

$$a_L = 0.83(\log L)^{2.414} \quad (10.9)$$

where

a_L is the apparent longitudinal dynamic dispersivity (L ; ft or m)

L is the length of the flow path (L ; ft or m)

Advection and Dispersion: Example

A landfill is leaking leachate with a chloride concentration of 725 mg/L, which enters an aquifer with the following properties:

$$\begin{aligned} \text{Hydraulic conductivity} &= 3.0 \times 10^{-3} \text{ cm/s } (3.0 \times 10^{-5} \text{ m/s}) \\ d_h/d_l &= 0.0020 \\ \text{Effective porosity} &= 0.23 \\ D^* &= 1 \times 10^{-9} \text{ m}^2/\text{s (estimated)} \end{aligned}$$

Compute the concentration of chloride in 1 y at a distance 15 m from the point where the leachate entered the ground water.

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Compute the concentration of chloride in 1 y at a distance 15 m from the point where the leachate entered the ground water.

- Determine average linear velocity.

$$v_L = \frac{K(d_h/d_l)}{n} = \frac{3.0 \times 10^{-5} \text{ m/s} \times 0.0020}{0.23} = 2.6 \times 10^{-7} \text{ m/s}$$

- Determine the coefficient of longitudinal hydrodynamic dispersion.

- Find the value of a_L from Equation 10.9

$$\begin{aligned} a_L &= 0.83 (\log L)^{2.454} \\ &= 0.83 (\log 15 \text{ m})^{2.454} \\ &= 1.23 \text{ m} \end{aligned}$$

- Find the value of D_L .

$$\begin{aligned} D_L &= a_L \times v_L + D^* \\ &= (1.23 \text{ m} \times 2.6 \times 10^{-7} \text{ m/s}) + 1 \times 10^{-9} \text{ m}^2/\text{s} \\ &= 3.2 \times 10^{-7} \text{ m}^2/\text{s} \end{aligned}$$

- Restate the 1-y time of travel in seconds.

$$\begin{aligned} t &= 1 \text{ y} \times 60 \text{ s/min} \times 1440 \text{ min/day} \times 365 \text{ days/y} \\ &= 3.15 \times 10^7 \text{ s} \end{aligned}$$

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Compute the concentration of chloride in 1 y at a distance 15 m from the point where the leachate entered the ground water.

- Substitute values into Equation 10.8.

$$\begin{aligned} C_0 &= 725 \text{ mg/L} \\ L &= 15 \text{ m} \\ t &= 3.15 \times 10^7 \text{ s} \end{aligned}$$

$$\begin{aligned} D_L &= 3.2 \times 10^{-7} \text{ m}^2/\text{s} \\ v_L &= 2.6 \times 10^{-7} \text{ m/s} \end{aligned}$$

$$\begin{aligned} C &= \frac{725}{2} \left\{ \operatorname{erfc} \left[\frac{15 \text{ m} - (2.6 \times 10^{-7} \text{ m/s} \times 3.15 \times 10^7 \text{ s})}{2 \sqrt{(3.2 \times 10^{-7} \text{ m}^2/\text{s} \times 3.15 \times 10^7 \text{ s})}} \right] \right. \\ &\quad \left. + \exp \left(\frac{2.6 \times 10^{-7} \text{ m/s} \times 15 \text{ m}}{3.2 \times 10^{-7} \text{ m}^2/\text{s}} \right) \right. \\ &\quad \left. \times \operatorname{erfc} \left[\frac{15 \text{ m} + (2.6 \times 10^{-7} \text{ m/s} \times 3.15 \times 10^7 \text{ s})}{2 \sqrt{(3.2 \times 10^{-7} \text{ m}^2/\text{s} \times 3.15 \times 10^7 \text{ s})}} \right] \right\} \text{ mg/L} \\ &= 362.5 \left[\operatorname{erfc} \left(\frac{15 \text{ m} - 8.19 \text{ m}}{6.3 \text{ m}} \right) + \exp(12.19) \times \operatorname{erfc} \left(\frac{15 \text{ m} + 8.19 \text{ m}}{6.3 \text{ m}} \right) \right] \text{ mg/L} \\ &= 362.5 [\operatorname{erfc}(1.08) + \exp(12.19) \times \operatorname{erfc}(3.68)] \text{ mg/L} \end{aligned}$$

The complementary error function can be determined from Appendix 13. Since the complementary error function of numbers greater than 3 is very small, we may ignore the second term of the equation.

$$\begin{aligned} C &= 362.5 \times 0.127 \text{ mg/L} \\ &= 46 \text{ mg/L} \end{aligned}$$

Adsorption – Ions “stick” to porous media and thus don’t advect or disperse

When an adsorption relationship can be plotted as a straight line on log-log paper, it is described by the Freundlich isotherm as

$$\log C^* = j \log C + \log K_f \quad (10.10)$$

or

$$C^* = K_f C^j \quad (10.11)$$

where

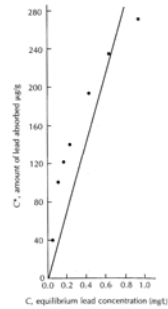
C^* = mass of solute sorbed per bulk unit dry mass of soil

C = solute concentration

K_f, j = coefficients

Lead Adsorption

► FIGURE 10.13
Lead adsorption by Cecil clay loam at pH 4.5 and at 25°C described by a linear Freundlich equation through the origin. Source: W. R. Ray, J. G. Kropec, S. F. J. Ochoa, & R. A. Griffin, Batch-Type Adsorption for Estimating Soil Attenuation of Chemicals, Technical Resource Document, EPA/330/3W-87-006, 1987.

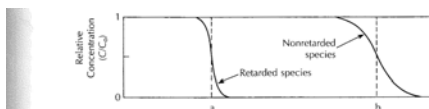


The slope of the curve on the log-log paper is represented by j . In a plot of C^* versus C , where the slope is a straight line, the relationship is linear, and j has a value of one. Under these conditions, the derivative of C^* with respect to C yields the relationship

$$dC^*/dC = K_d \quad (10.12)$$

where K_d is known as a **distribution coefficient**.

Influence of Adsorption



▲ FIGURE 10.14
Influence of retardation on movement of a solute front in a one-dimensional column.

Retardation

The K_d value can be used to compute the retardation of the solute front as it passes through the soil by the following equation:

$$\text{Retardation factor} = 1 + (\rho_b/\theta)(K_d) \quad (10.14)$$

where

ρ_b is dry bulk mass density of the soil (M/L^3 ; gm/cm^3)

θ is volumetric moisture content of the soil (dimensionless)

K_d is distribution coefficient for the solute with the soil (L^2/M ; mL/g)

If a solute is reactive, it will travel at a slower rate than the ground water owing to adsorption. The rate of solute movement can be determined by the retardation equation

$$v_r = v_a/[1 + (\rho_b/\theta)(K_d)] \quad (10.15)$$

where

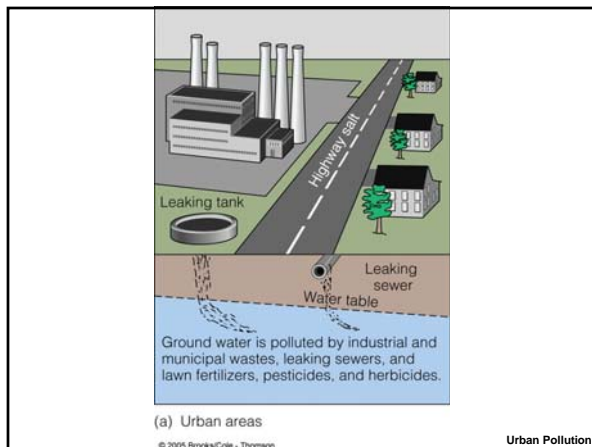
v_a is average linear velocity (L/T ; ft/day or m/day)

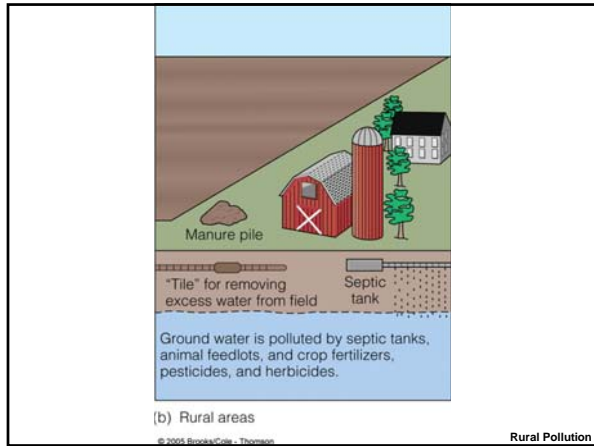
v_r is velocity of the solute front. In a one-dimensional column the solute concentration is one-half of the original value ($C/C_0 = 0.5$) (L/T ; ft/day or m/day)

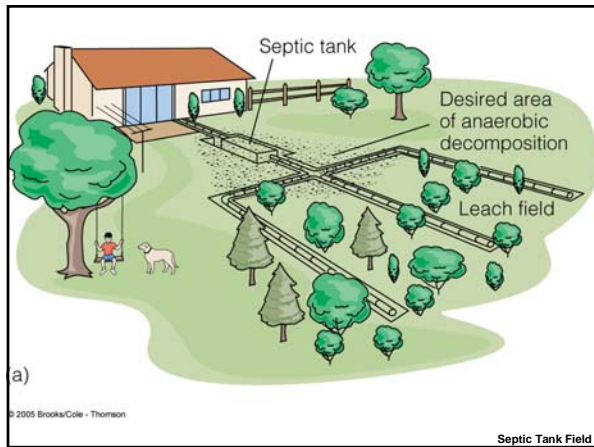
Retardation Example

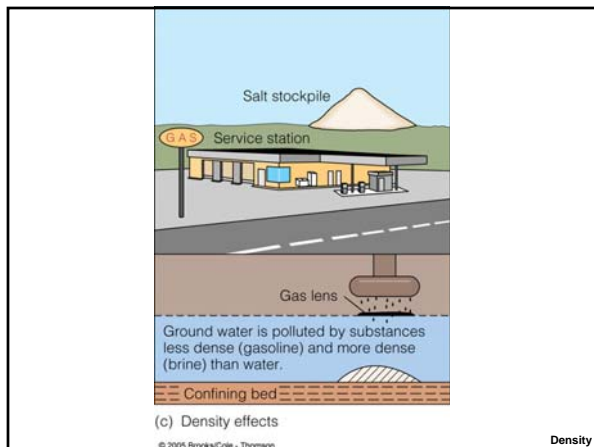
Compute the relative velocity of the solute front of a solute-soil system with a distribution coefficient of 10 mL/g , a ρ_b value of 1.75 g/cm^3 , and θ of 0.20 .

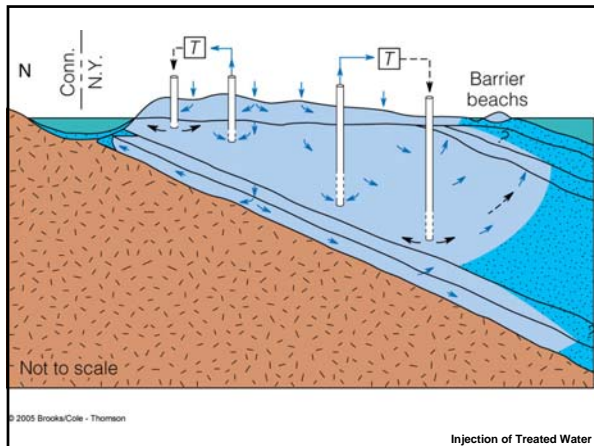
$$\begin{aligned} v_r &= \frac{v_a}{1 + (\rho_b/\theta)(K_d)} \\ &= \frac{v_a}{1 + \left(\frac{1.75 \text{ g/cm}^3}{0.20}\right) \left(\frac{10 \text{ mL}}{\text{g}}\right) \left(\frac{1 \text{ cm}^3}{1 \text{ mL}}\right)} \\ &= \frac{v_a}{88.5} \\ &= 0.011 v_a \end{aligned}$$











Organic Pollutants

Table 10.3 Solubility, K_{ow} , and mobility class for common organic pollutants

Compound	Solubility (mg/L)	K_{ow} (mL/g)	Mobility Class
1,4-Dioxane	miscible	1	very high
4-hydroxy-4-methyl-2-pentanone	miscible	1	very high
acetone	miscible	1	very high
tetrahydrofuran	miscible	1	very high
NN-dimethylformamide	1	1	very high
NN-dimethylacetamide	2	2	very high
2-methyl-2-butanol	14000	6	very high
2-butanol	125000	6	very high
ethyl ether	84300	8	very high
cyclohexanol	56700	10	very high
3-methylbutanoic acid	42300	12	very high
benzyl alcohol	40000	12	very high
aniline	34000	13	very high
2-hexanone (butylmethylketone)	35000	14	very high
2-hydroxy-triethylamine	31000	15	very high
2-methylphenol (o-cresol)	31000	15	very high
2-methyl-2-propanol		16	very high

Organic Pollutants

Table 10.3 continued

Compound	Solubility (mg/L)	K_{ow} (mL/g)	Mobility Class
4-methylphenol (p-cresol)	24000	17	very high
pentanoic acid	24000	17	very high
cyclohexanone	23000	18	very high
4-methyl-2-pentanone	19000	20	very high
2,4-dimethyl phenol	17000	21	very high
4-methyl-2-pentanol	17000	21	very high
methylene chloride	13200	25	very high
isophorone	12000	26	very high
phenol	82000	27	very high
2-chlorophenol	11087	27	very high
hexanoic acid	11000	28	very high
chloroform	7840	34	very high
1,2-dichloroethane	8450	36	very high
1,2-trans-dichloroethene	6300	39	very high
chloroethane	5700	42	very high
5-methyl-2-hexanone	5400	43	very high
chloroethane	5380	43	very high
1,1-dichloroethane	5100	45	very high
1,1,2-trichloroethane	4420	49	very high

Organic Pollutants

1,2-dichloropropane	3570.	51	high
benzoic acid	2900.	64	high
octanoic acid	2500.	70	high
heptanoic acid	2410.	71	high
1,1,2,2-tetrachloroethane	3230.	88	high
benzene	1780.	97	high
diethyl phthalate	1000.	123	high
2-nonanol	1000.	123	high
bromodichloromethane	900.	131	high
3-methylbenzoic acid	850.	136	high
trichloroethene	1100.	152	moderate
1,1,1-trichloroethane	700.	155	moderate
di-n-butyl phthalate	400.	217	moderate
1,1-dichloroethene	400.	217	moderate
carbon tetrachloride	800.	232	moderate
2-butanone (methyl ethyl ketone)	353.	235	moderate
4-methylbenzoic acid	340.	240	moderate
toluene	500.	242	moderate
tetrachloroethylene	200.	303	moderate
chlorobenzene	448.	318	moderate
1,2-dichlorobenzene	148.	343	moderate
o-xylene	170.	363	moderate
1,2,2-trifluoro-1,1,2-trichloroethane		372	moderate
styrene	162.	380	moderate
1,3-dichlorobenzene	118.	463	moderate
fluorotrichloromethane	110.	476	moderate
4,6-dinitro-2-methylphenol		477	moderate

Organic Pollutants

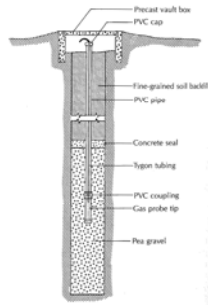
N-nitrosodiphenylamine	35.1	982	low
3,5-dimethylphenol		1038	low
gHC-delta	31.5	1052	low
2,6-dimethylphenol		1060	low
1,2,4-trichlorobenzene	30.	1080	low
naphthalene	31.7	1300	low
4-ethylphenol		1986	low
dibenzofuran	10.	2140	slight
hexachloroethane	8.	2450	slight
acenaphthene	7.4	2580	slight
gg-N-propylamine		2610	slight
BHC-alpha	8.5	2627	slight
BHC-beta	2.7	3619	slight
hexachlorobenzene	0.035	3910	slight
hexachlorobutadiene	3.2	4330	slight
di-n-octyl phthalate	3.	4510	slight
butyl benzyl phthalate	2.9	4606	slight
fluorene	1.98	5835	slight
2-methylnaphthalene	25.4	8500	slight
bis(2-ethylhexyl)phthalate	0.6	12200	slight
toxaphene	0.4	15700	slight
heptachlor epoxide	0.35	17087	slight
endosulfan II	0.28	19623	slight
fluoranthene	0.275	19800	slight

Organic Pollutants

1,2-diphenylhydrazine (as azobenzene)	0.252	20947	immobile
endosulfan sulfate	0.22	22788	immobile
phenanthrene	1.29	23000	immobile
dieldrin	0.188	25120	immobile
anthracene	0.073	26000	immobile
BHC-gamma	0.15	28900	immobile
decanoic acid		39610	immobile
chlordane	0.056	53200	immobile
pyrene	0.135	63400	immobile
PCB-1254	0.042	63914	immobile
heptachlor	0.03	78400	immobile
endrin	0.024	90000	immobile
benzo(a)anthracene	0.014	125719	immobile
aldrin	0.013	132000	immobile
4,4'-DDE	0.01	155000	immobile
4,4'-DDT	0.0017	238000	immobile
4,4'-DDD	0.005	238000	immobile
benzo(o)pyrene	0.0038	282185	immobile
PCB-1260	0.0027	349462	immobile
chrysene	0.022	420108	immobile
benzo(j)fluoranthene		1148497	immobile
benzo(i)fluoranthene		2020971	immobile

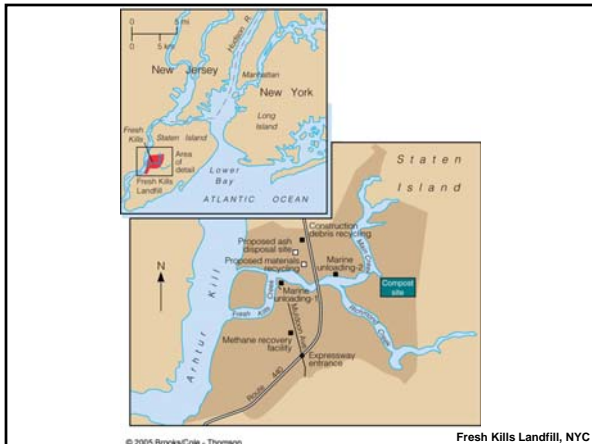
Gas Monitoring Well

► FIGURE 10.6
Gas monitoring well in vadose zone.
Source: L. S. Wilson, *Ground Water Monitoring Review 2*, no. 1 (1982):
155-66.

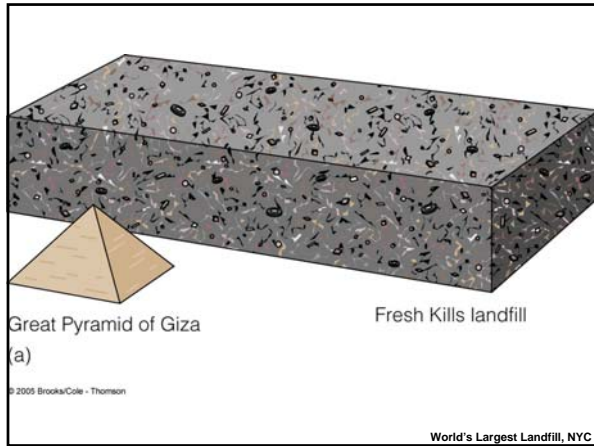




© 2005 Brooks/Cole - Thomson
Full, graded landfill prior to planting



© 2005 Brooks/Cole - Thomson
Fresh Kills Landfill, NYC



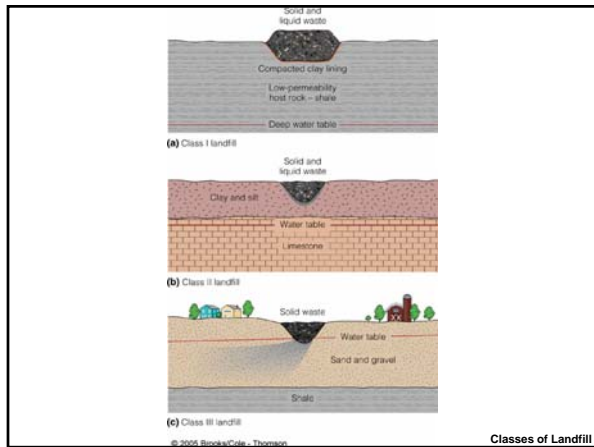


TABLE 15.1 Classifications of Disposal Sites and Waste Groups	
Geology of Disposal Sites	
Class I	No possibility of discharge of leachate to usable waters. Inundation and washout must not occur. The underlying lining material, whether soil or synthetic, must be essentially impermeable; that is, it must have a permeability less than 0.3 cm/year. All waste groups may be received (Figure 15.5, part a).
Class II	Site overlies or is adjacent to usable ground water. Artificial barriers may be used for both vertical and lateral leachate migration. Geologic formation or artificially constructed liners or barriers should have a permeability of less than 30 cm/year. Groups 2 and 3 waste may be accepted (Figure 15.5, part b).
Class III	Inadequate protection of underground- or surface-water quality. Includes filling of areas that contain water, such as marshy areas, pits, and quarries. Only inert Group 3 wastes can be accepted (Figure 15.5, part c).
Constituents of Waste Groups	
Group 1	Consists of but not limited to toxic substances that could impair water quality. Examples are saline fluids, toxic chemicals, toilet wastes, brines from food processing, pesticides, chemical fertilizers, toxic compounds of arsenic, and chemical-warfare agents.
Group 2	Household and commercial garbage, tin cans, metals, paper products, glass, cloth, wood, yard clippings, small dead animals, and hair, hide, and bones.
Group 3	Non-water-soluble, nondecomposable inert solids such as concrete, asphalt, plasterboard, rubber products, steel-mill slag, clay products, glass, and asbestos shingles.



